



# Calculating Simple and Compound Interest



## The Simple Interest Formula

Simple interest is based on a percentage of the principal borrowed. You can calculate it using the following formula:

$$\text{Simple Interest: } SI = P \times r \times t$$

$SI$  = Simple Interest

$P$  = Principal (amount borrowed or invested)

$r$  = rate of interest

$t$  = time (how many years you borrow the money for)

**Note:** For time less than a year, use a decimal. Ex: 6 months is half of a year, or 0.5

Let's look at an example. Say you borrowed \$800 and agreed to repay that amount at 6% simple interest in 1 year.

It's good to first list the values for each variable in the formula. Here,  $P = \$800$ ,  $r = 6\% = 0.06$ , and  $t = 1$  year. So, you'd end up with:

$$SI = \$800 \times 0.06 \times 1$$

$$SI = \$48 \times 1$$

$$SI = \$48$$

This shows us that it costs \$48 for you to borrow \$800 for one year with these terms. If you borrowed the money for two years under the same conditions, you would owe twice that amount, or \$96 in interest.

## The Compound Interest Formulas

Compound interest is based on a percentage of the principal borrowed, plus the accrued interest. You can calculate it using the following formula:

$$\text{Compound Interest: } CI = P \left(1 + \frac{r}{n}\right)^{nt} - P$$

$P$  = Principal (amount borrowed or invested)

$r$  = rate of interest

$n$  = number of times the interest is compounded every year

$t$  = time (number of years you borrow the money for)

Here's an example of how the formula works. You get \$200 for your birthday and decide to put it into a high-yield savings account earning 3% compounded monthly. How much will you earn in 4 years?

The compound interest formula might look a bit complex. But we'll do some initial calculations first, in order to make the final calculations easier.

**Step 1:** Convert the annual interest rate (3%, or 0.03) to a monthly rate:

$$\frac{r}{n} = \frac{0.03}{12} = 0.0025$$

**Step 2:** Calculate your exponent. (number of times interest is compounded  $\times$  number of years.)

$$nt = 12 \times 4 = 48$$

**Step 3:** Insert your calculations for  $\frac{r}{n}$  and  $nt$  into the formula, along with the original amount (principal),  $P = 200$ .

$$A = CI = \$200 (1 + 0.0025)^{48}$$

**Step 4:** Use the order of operations (PEMDAS) to solve your equation.

$$\begin{aligned} CI &= 200 (1 + 0.0025)^{48} - 200 \\ CI &= 200 (1.0025)^{48} - 200 \text{ (parentheses)} \\ CI &= 200 (1.127328) - 200 \text{ (exponent)} \\ CI &= 225.47 - 200 \text{ (multiply)} \\ CI &= 25.47 \text{ (subtract)} \end{aligned}$$

At the end of 4 years, you'll have earned \$25.47. And you'll have a total of \$225.47 in your account — the original \$200 plus \$25.47 in interest.

## Check Your Understanding

Using the formulas above, find the answer for each of the following problems

1. Sara is investing \$250 in a certificate at 5.4% simple interest. How much will she earn when it matures in 18 months?
2. Juan is buying his first car. He's offered a loan of \$20,000 at 11.91% simple interest for 36 months. How much will he pay in interest?
3. Maya has \$500 to invest. Credit union A offers a simple interest rate of 5%. Credit union B offers an account with a 4.75% rate, compounded monthly. Which account would help him earn the most money over a period of 4 years?

## Check Your Understanding Answers

1. \$20.25

2. \$7,146.00

3. **Interest earned:**

Credit union A: \$100; credit union B: \$104.40

**Credit union B will return \$4.40 more in 4 years.**